

1. Find each of the following derivatives. You may use the rules from class. NO need to simplify!

a. $f(x) = x^4 + 23x^3 - \frac{1}{x}$. $f'(x) = 4x^3 + 69x^2 + x^{-2} - x^{-1} = 4x^3 + 69x^2 + \frac{1}{x^2}$ ← *4 missed*

b. $y = (3x^4 - x^3 + x^2 - 10)(20x^6 - 2x^5 + 2x)$. $\frac{dy}{dx} =$
 $(3x^4 - x^3 + x^2 - 10)(120x^5 - 10x^4 + 2) + (20x^6 - 2x^5 + 2x)(12x^3 - 3x^2 + 2x)$ *3 missed*

c. $f(x) = (x^2 + 2)^2$. $f'(x) = 4x^3 + 8x$
 $(x^2 + 2)(x^2 + 2) = (x^4 + 4x^2 + 4)$ *all but 3*

d. $z = \frac{x^2 - 1}{x^2 + x}$. $\frac{dz}{dx} = \frac{(x^2 + x)(2x) - (x^2 - 1)(2x + 1)}{(x^2 + x)^2}$
one guy forgot (x+1) *all but 6*

2. What is the equation of the straight line tangent to the curve $y = 3x^4 - x$ at $(1, 2)$?

$\frac{dy}{dx} = 12x^3 - 1$
 $(1, 2)$ $m = 12 - 1 = 11$
 $y - 2 = 11(x - 1)$
 $y - 2 = 11x - 11$
 $y = 11x - 9$ *all but 3*

3. Use the quotient rule to show that for $f(x) = x^{-4}$, $f'(x) = \frac{-4x^{-5}}{1 \cdot x^0}$. (and fill in) *power formula needs*

$f(x) = \frac{1}{x^4}$
 $f'(x) = \frac{x^4(0) - 1(4x^3)}{x^8} = \frac{-4x^3}{x^8} = -4x^{-5}$ *all but 4*

4. Suppose the height (ft.) above ground of an object under free fall is given by $h = 200 + 20t - 16t^2$, where t is time in seconds, $t \geq 0$. (Give units of answers) *many thought this is "drops"*

a. Find a formula for the velocity.

$v = \frac{dh}{dt} = 20 - 32t$

b. What is the velocity at $t = 2$ sec.? Is (it) going up or down? How do you know? *object*

$v = 20 - 32(2) = 20 - 64 = -44$ ft/sec down

c. Find a formula for the acceleration.

$a = \frac{dv}{dt} = -32$ ft/sec²

d. How high does (it) go? Show work.

$v = 0$ $20 - 32t = 0$
 $t = \frac{20}{32} = \frac{5}{8}$
 $h = 206.25$ *all but 19 got all*