

Wed 2/5/85
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1. Find the components of the vector with initial point (2,-1) and terminal point (-3,4).

$$\begin{pmatrix} -3-2 \\ 4-(-1) \end{pmatrix} = \begin{pmatrix} -5 \\ 5 \end{pmatrix}$$

2. Given the vectors $\vec{u} = (2,1,3)$, and $\vec{v} = (-2,2,1)$, find:

a. $\vec{u} + \vec{v} = (0, 3, 4)$

b. $3\vec{u} = (6, 3, 9)$

c. $|\vec{v}| = \sqrt{2^2 + 2^2 + 1^2} = 3$

d. $\vec{u} \cdot \vec{v} = 2(-2) + 1(2) + 3(1) = -4 + 5 = 1$

f. $3\vec{u} + 6\vec{v} = \begin{pmatrix} 6 \\ 3 \\ 9 \end{pmatrix} + \begin{pmatrix} -12 \\ 12 \\ 6 \end{pmatrix} = \begin{pmatrix} -6 \\ 15 \\ 15 \end{pmatrix}$

e. the orthogonal projection of \vec{u} onto \vec{v} is

$$\frac{\vec{u} \cdot \vec{v}}{\vec{v} \cdot \vec{v}} \vec{v} = \frac{1}{9} (2, 2, 1) = \left(\frac{2}{9}, \frac{2}{9}, \frac{1}{9} \right)$$

3. Find the equation of the plane through the point (0,2,-1) which is parallel to the plane

$$x - 2y + z = 5.$$

$$\vec{n} = (1, -2, 1)$$

$$(1, -2, 1) \cdot (x-0, y-2, z+1) = 0$$

$$x - 2(y+2) + z + 1 = 0$$

$$x - 2y + z = -5$$

4. Are the vectors $\vec{a} = (1,2,-3)$ and $\vec{b} = (2,1,1)$ orthogonal? Justify.

$$(1, 2, -3) \cdot (2, 1, 1)$$

$$= 2 + 2 - 3 = 1 \neq 0$$

NO.